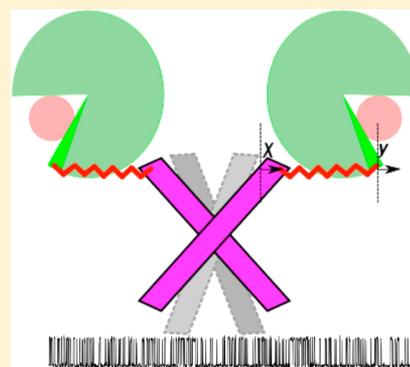


Mechanism-Based Mathematical Model for Gating of Ionotropic Glutamate Receptors

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ABSTRACT: We present a mathematical model for ionotropic glutamate receptors (iGluR's) that is built on mechanistic understanding and yields a number of thermodynamic and kinetic properties of channel gating. iGluR's are ligand-gated ion channels responsible for the vast majority of fast excitatory neurotransmission in the central nervous system. The effects of agonist-induced closure of the ligand-binding domain (LBD) are transmitted to the transmembrane channel (TMC) via interdomain linkers. Our model demonstrates that, relative to full agonists, partial agonists may reduce either the degree of LBD closure or the curvature of the LBD free energy basin, leading to less stabilization of the channel open state and hence lower channel open probability. A rigorous relation is derived between the channel closed-to-open free energy difference and the tension within the linker. Finally, by treating LBD closure and TMC opening as diffusive motions, we obtain gating trajectories that resemble stochastic current traces from single-channel recordings and calculate the rate constants for transitions between the channel open and closed states. Our model can be implemented by molecular dynamics simulations to realistically depict iGluR gating and may guide functional experiments in gaining deeper insight into this essential family of channel proteins.



including higher order processes such as learning and memory. These tetrameric assemblies convert agonist (glutamate or glycine) binding to the ligand-binding domain (LBD) into currents through the transmembrane channel (TMC; Figure 1A).^{3–5} iGluR subunits are composed of discrete, highly modular domains that are separated from each other by flexible linkers.^{6,7} The extracellular LBD is composed of two lobes termed D1 and D2. The LBDs from various iGluR subunits have been genetically isolated and crystallized in an assortment of ligand-bound forms.⁵ The transmembrane domain consists of three transmembrane helices (termed M1, M3, and M4) and a re-entrant helix (termed M2). The TMC is formed by the tetrameric assembly of the transmembrane domains of the receptor's four subunits, with M3 as the major pore-lining helix and forming the activation gate at the C-terminus.^{3,6} The M2–M3 region has some similarity in sequence and structure with the counterpart in potassium channels.^{6,8,9}

INTRODUCTION

Transmembrane proteins that form ion channels receive stimuli to open a pore and allow the passage of ions. This process, termed gating, is frequently modeled at three different levels. Kinetic models derived from single-channel or whole-cell recordings provide phenomenological descriptions of channel activity but cannot capture molecular details underlying the kinetic steps. Structural models of gating, either from structure determination (e.g., X-ray crystallography) at putatively different functional states or from mutagenesis-based (e.g., cysteine substitution) functional studies, provide qualitative descriptions of the crucial movements involved in gating but cannot inform how the energetics and dynamics of the relevant structural elements quantitatively define the gating process. Computational models, e.g., from molecular dynamics simulations, can capture some of the energetics and dynamics but are inevitably limited in the temporal and conformational scales that can be explored. A fourth type of model,^{1,2} termed mathematical here, allows thermodynamic and kinetic properties of the gating process to be calculated from the energetics and dynamics of the conformational changes involved, thus bridging some of the gaps in the preceding three types of models. The present study aims to present such a mathematical model for ionotropic glutamate receptors (iGluR's).

iGluR's are ligand-gated ion channels responsible for the vast majority of fast excitatory neurotransmission in the central nervous system. The two main iGluR subtypes, AMPA and NMDA receptors, are essential to all aspects of brain function

The gating mechanisms of iGluR's have been studied extensively. Kinetic modeling of single-channel and whole-cell currents reveals complex behavior, including multiple open and closed substates at saturating agonist concentrations.^{10–16} Crystal structures of isolated LBDs and near-full-length receptors^{6,17–20} have clearly defined the agonist-induced lobe

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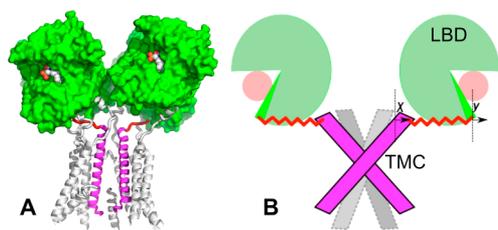


Figure 1. Structure of an AMPA receptor and our mechanism-based mathematical model. (A) Crystal structure of an AMPA receptor (Protein Data Bank entry 3KG2). The LBD is rendered as a green surface; bound ligand is shown as spheres; the TMC is shown as a cartoon, with one subunit undisplayed for clarity. The M3 helices from two diagonal subunits are highlighted in magenta and the corresponding M3–D2 linkers highlighted in red. (B) Model for channel gating. The agonist-bound LBD can be closed (dark green) or transiently open (light green); y denotes the degree of LBD closure (the 0 value of y , where the LBD free energy is at a minimum, is indicated by a vertical line next to the symbol “ y ”). The C-termini of the M3 helices move outward (inward) to open (close) the channel; x denotes the degree of channel opening (the 0 value of x is indicated by a vertical line next to the symbol “ x ”). The distance between the two vertical lines is L_0 . When x and y are displaced from their 0 values, $L_0 + y - x$ is the length of the linker.

closure of the LBD and also suggested a crucial role for the LBD–TMC linkers, especially the M3–D2 linker, in transmitting the effect of agonist binding further to the TMC but have revealed little about the conformations adopted by the TMC in the open state. On the other hand, functional data based on cysteine substitution have shown that the M3 helix is an essential component of iGluR pore opening and appears to be largely rigid,^{21–23} but structural elements around M3 also significantly contribute to the activation process.^{24,25} In addition, molecular dynamics simulations^{26,27} have presented a likely scenario for the coupling between LBD lobe closure and TMC pore opening: the closure of the D2 lobe toward D1 produces outward pulling of the M3–D2 linker, which in turn leads to channel opening (Figure 1). This coupling mechanism was further addressed in a combined functional and computational study,¹⁶ which showed that glycine insertions in the M3–D2 linker designed to increase the linker length and hence weaken the LBD–TMC coupling significantly reduced the channel open probability. Also contributing to our understanding of channel gating are free energy calculations for the

LBD lobe closure through molecular dynamics simulations.^{28–30}

Here, building on the significant mechanistic understanding achieved so far on iGluR gating, we present a mathematical model for calculating thermodynamic and kinetic properties of the gating process from the energetics and dynamics of intra- and interdomain motions. We show illustrative results on partial agonism, effects of linker insertions, and transition rates between channel open and closed states.

THE MODEL

We model the energetics for the lobe closure of the agonist-bound LBD and the pore opening of the TMC, as well as their coupling by the M3–D2 linker (Figure 1B). The free energy surface for LBD closure has been calculated through molecular dynamics simulations.^{28–30} To model the single well of this free energy surface, we use a harmonic potential

$$W_b(y) = \frac{1}{2}k_b y^2 \quad (1)$$

where y is the degree of LBD closure, with $y = 0$ corresponding to the free energy minimum and negative y signifying opening of the agonist-bound LBD, and k_b is the LBD spring constant. Similarly, we model the small-amplitude extension and contraction of the M3–D2 linker from its optimal length L_m by a harmonic potential

$$W_l(x, y) = \frac{1}{2}k_l(y - x + \Delta)^2 \quad (2)$$

where x is the degree of TMC opening; $\Delta = L_0 - L_m$, with L_0 denoting the length of the linker at $x = y = 0$; and k_l is the linker spring constant.

We assume that the TMC has a global minimum corresponding to the closed state and a shallow minimum corresponding to the open state; the quiescent channel predominantly stays in the closed state but may make rare excursions to the open state. This is captured by the potential (Figure 2A)

$$W_c(x) = \varepsilon[(x^2 - 1)^2 - x^3/3 + x] \quad (3)$$

which has the global and shallow minima located at $x = -1$ and $x = 1$, respectively, with a free energy difference of $4\varepsilon/3$. The free energy for the receptor as a whole is then

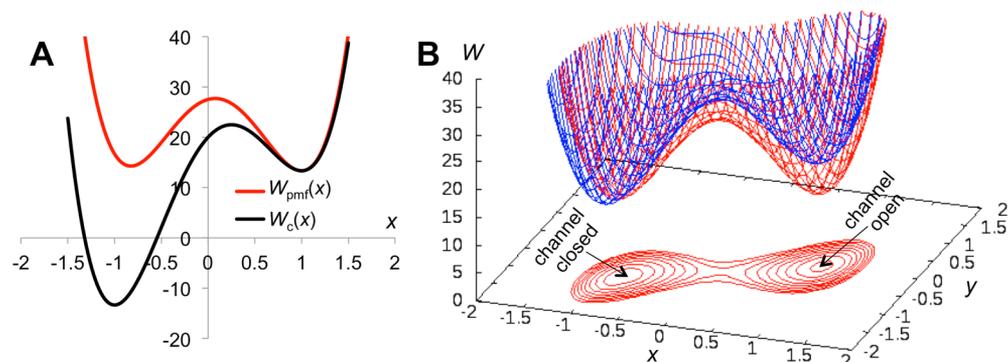


Figure 2. Free energy surface of the receptor. (A) The free energy function of the isolated TMC and the potential of mean force for TMC opening when coupled to the LBD via the M3–D2 linker. (B) The free energy surface for the receptor. Shown in red is the free energy surface (also displayed as contours) when the LBD is bound with a full agonist. In blue is the free energy surface when the LBD is bound with an NMDAR-type partial agonist, which reduces the curvature (i.e., k_b) of the free energy function for LBD closure (from 30 to 20).

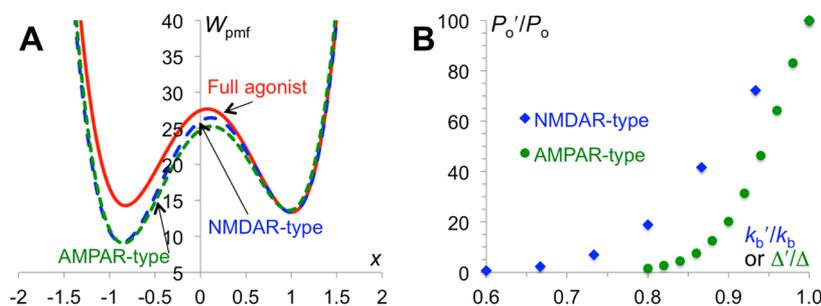


Figure 3. Partial agonism. (A) Potentials of mean force for full and AMPAR-type (reduced degree of cleft closure) and NMDAR-type (reduced curvature of LBD free energy basin) partial agonists. (B) Relative efficacies of the two types of partial agonists.

$$W(x, y) = W_c(x) + W_l(x, y) + W_b(y) \quad (4)$$

The two-dimensional free energy surface at $\varepsilon = 20$, $k_b = k_l = 30$, and $\Delta = 1$ is shown in Figure 2B. All energies are measured in units of the product of Boltzmann's constant and absolute temperature, and lengths are in units of Å. The chosen value of Δ is such that the linker is in its relaxed state (i.e., neither compressed nor extended) when the LBD is at its free energy minimum (i.e., $y = 0$) and the TMC is at its open state minimum (i.e., $x = 1$). If the TMC were to move toward the closed state, the linker would be extended, resulting in an energetic penalty. The LBD–TMC coupling via the linker therefore leads to an overall free energy surface that has two nearly evenly matched minima, one at $(x, y) = (1, 0)$ for the channel open state and the other at $(-0.83, -0.91)$ for the channel closed state. The stabilization effect on the channel open state by the coupling to the LBD can be seen by comparing the free energy function $W_c(x)$ of the isolated TMC with the potential of mean force, $W_{pmf}(x)$, in x for the full receptor (Figure 2A), defined through

$$e^{-W_{pmf}(x)} = C \int dy e^{-W(x, y)} \quad (5)$$

With an appropriate choice of the arbitrary normalization constant C , the resulting potential of mean force is

$$W_{pmf}(x) = W_c(x) + \frac{k_b k_l}{2(k_b + k_l)} (x - \Delta)^2 \quad (6)$$

The second term on the right-hand side of eq 6 arises from the coupling to the LBD. Its value is 0 at $x = \Delta = 1$ and positive at $x = -1$.

The two stable states are separated by a saddle-shaped barrier. The lowest barrier heights, located at the saddle point $(0.076, -0.46)$, are 14.4 and 13.4 when measured from the channel open and closed minima, respectively. These will be denoted as $\Delta W_{o \rightarrow sp}$ and $\Delta W_{c \rightarrow sp}$, respectively.

RESULTS

Our model predicts a number of important functional properties of iGluR gating, allowing for validation and refinement by future electrophysiological measurements.

Partial Agonism. Full agonists evoke maximal currents through the TMC, whereas partial agonists have submaximal efficacy. Partial agonism manifests itself first through the LBD, and this manifestation has been the subject of many experimental and computational studies.^{29,31–43} For AMPA receptors, a correlation between the degree of LBD closure and agonist efficacy was observed in crystal structures.^{33,37} This correlation is absent in NMDA receptors, as their LBDs bound

with full and partial agonists have very similar structures.^{34–36,42} Recently, we found that the GluN1 LBD responds to partial agonist binding by reducing the curvature of the free energy surface while largely preserving the minimum position.²⁸

How is partial agonism transmitted to the TMC to produce submaximal currents? We can now directly address this question with our model. Agonist efficacy can be measured by the channel open probability,^{15,44} which in our model is given by

$$P_o = \frac{\int_{x > x^\ddagger} dx e^{-W_{pmf}(x)}}{\int dx e^{-W_{pmf}(x)}} \quad (7)$$

where x^\ddagger denotes the barrier of the potential of mean force separating the channel open and closed states. For AMPA receptors, reduced closure of the LBD by a partial agonist would lead to compression of the linker if the TMC is in the open state; the strain in the linker would be relieved if the TMC retracts to the closed state (Figure 1B). This effect can be illustrated by reducing L_0 and hence Δ by 0.2. The potentials of mean force for the full and AMPAR-type partial agonists are compared in Figure 3A. Correspondingly, the channel open probability is reduced from 0.71 to 0.011. The dependence of the relative efficacy, defined as P_o'/P_o , on Δ'/Δ is shown in Figure 3B; the unprimed and primed symbols denote quantities related to the full and partial agonists, respectively.

For the NMDAR-type partial agonists, following our earlier study,²⁸ we assume that the curvature of the LBD free energy function is reduced. As a result, the penalty for moving away from the LBD-closed conformation (i.e., $y = 0$) is lowered; when coupled to the TMC via the linker, the stabilization of the channel open state is correspondingly less. The two-dimensional free energy surface for an NMDAR-type partial agonist, with k_b reduced from 30 to 20, is illustrated in Figure 2B. The resulting potential of mean force in x is compared to that for the full agonist in Figure 3A. This partial agonist reduces the channel open probability from 0.71 to 0.016. The dependence of the relative efficacy on k_b'/k_b is shown in Figure 3B.

Linker Insertions. Molecular dynamics simulations have shown that the M3–D2 linker is critical for transmitting the effect of the agonist-induced LBD conformational change to the TMC.^{26,27} To directly probe the role of the M3–D2 linker, Kazi et al.¹⁶ introduced glycine insertions. The resulting lengthening of the linker was found to reduce the channel open probability. We can explain this observation with our model by noting that a glycine insertion would increase L_m , the optimal linker length. As a result, Δ is decreased. The net effect of the glycine insertion is thus identical to that of an AMPAR-type partial agonist.

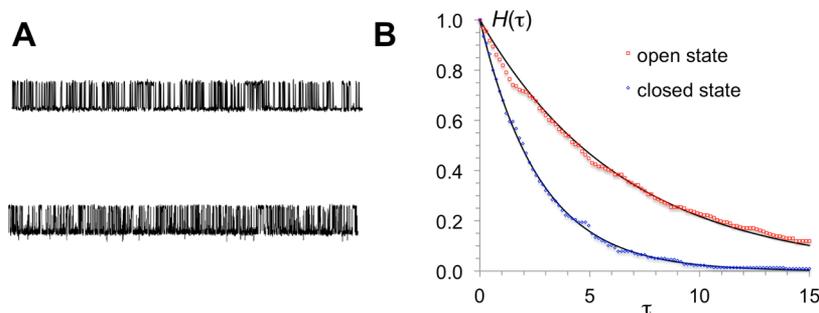


Figure 4. “Current” traces and channel open and closed times. (A) Upper trace: values of x from a Brownian dynamics simulation of the model at $D_x = D_y = 2 \times 10^4$, using the Ermak–McCammon algorithm⁴⁵ with a time step of 5×10^{-8} . Lower trace: currents from a single-channel recording of the GluN1/GluN2A NMDA receptor under steady-state conditions at pH 8 in the on-cell attached configuration. (B) Probabilities for residence times in channel open and closed states to be longer than τ . Symbols are from binning the residence times from the simulation; curves are single exponentials with exponents given by the mean residence times in the channel open and closed states.

Kazi et al.¹⁶ empirically interpreted the change in the closed-to-open free energy difference, $\Delta G_{c \rightarrow o}$, by a glycine insertion in terms of the tension in the linker. With our model, we can derive a rigorous relation between insertion-induced change in $\Delta G_{c \rightarrow o}$ and linker tension. We first note that a spring (with spring constant k_l) when extended by δ generates a tension $k_l \delta$ within. Hence, to find the tension within the linker, we need to calculate the average extension of the linker. When the channel is in the closed state, the average extension is

$$\delta_c = \frac{\int_c dx dy e^{-W(x,y)} (y - x + \Delta)}{\int_c dx dy e^{-W(x,y)}} \quad (8)$$

where the subscript “c” in the integrals signifies that the area of integration is restricted to the channel closed state. Similarly, the average extension of the linker in the channel open state is

$$\delta_o = \frac{\int_o dx dy e^{-W(x,y)} (y - x + \Delta)}{\int_o dx dy e^{-W(x,y)}} \quad (9)$$

In our model with $k_b = 30$ and $\Delta = 1$, the average linker extensions are 0.01 and 0.91, respectively, in the channel open and closed states. That is, the linker is more extended and hence there is greater tension in the channel closed state.

The closed-to-open free energy difference is given by

$$e^{-\Delta G_{c \rightarrow o}} = \frac{\int_o dx dy e^{-W(x,y)}}{\int_c dx dy e^{-W(x,y)}} \quad (10)$$

or

$$\Delta G_{c \rightarrow o} = -\ln \int_o dx dy e^{-W(x,y)} + \ln \int_c dx dy e^{-W(x,y)} \quad (11)$$

We now take the derivative of $\Delta G_{c \rightarrow o}$ with respect to the linker optimal length L_m :

$$\begin{aligned} \frac{\partial \Delta G_{c \rightarrow o}}{\partial L_m} &= -\frac{k_l \int_o dx dy e^{-W(x,y)} (y - x + \Delta)}{\int_o dx dy e^{-W(x,y)}} \\ &+ \frac{k_l \int_c dx dy e^{-W(x,y)} (y - x + \Delta)}{\int_c dx dy e^{-W(x,y)}} \end{aligned} \quad (12)$$

Using eqs 8 and 9, we can simplify the last result as

$$\frac{\partial \Delta G_{c \rightarrow o}}{\partial L_m} = -k_l \delta_o + k_l \delta_c \quad (13)$$

Note that $k_l \delta_o$ and $k_l \delta_c$ can be recognized as the linker tensions in the channel open and closed states, respectively, to be denoted as F_o and F_c . For a small change in L_m , denoted as δL_m , the preceding equation allows us to find the corresponding change in $\Delta G_{c \rightarrow o}$ as

$$\delta \Delta G_{c \rightarrow o} = (F_c - F_o) \delta L_m \quad (14)$$

That is, the insertion-induced change in $\Delta G_{c \rightarrow o}$, when divided by the change in linker optimal length, is equal to the difference in linker tension between the channel closed and open states in the wild-type receptor. Since our model predicts $F_c > F_o$, a linker insertion leads to an increase in $\Delta G_{c \rightarrow o}$, i.e., a decrease in channel open probability. This is just what was observed by Kazi et al.¹⁶

Single-Channel Gating Kinetics. So far we have only dealt with equilibrium properties. By assuming appropriate dynamics for the two coordinates x and y , our model can also predict kinetic properties of channel gating. Here we assume that x and y follow diffusive dynamics, with diffusion constant D_x and D_y , respectively. A trajectory with many transitions between the channel closed and open states then resembles the stochastic current trace of a single-channel recording (Figure 4A). The probabilities, $H_o(\tau)$ and $H_c(\tau)$, that the residence times in the channel open and closed states are longer than τ compare well with single exponentials, $\exp(-\tau/\bar{\tau}_o)$ and $\exp(-\tau/\bar{\tau}_c)$, respectively (Figure 4B), as can be expected owing to the high energy barriers that must be crossed in order to leave the energy wells. With D_x and D_y set to 2×10^4 (in units of $\text{\AA}^2/\text{ms}$), the mean residence times, $\bar{\tau}_o$ and $\bar{\tau}_c$, are 6.6 and 2.7 (in units of ms), in the channel open and closed states, respectively. Note that the ratio $\bar{\tau}_o/(\bar{\tau}_o + \bar{\tau}_c)$ agrees well with P_o , confirming that the trajectory represents an equilibrium sampling of the free energy surface.

The inverses of $\bar{\tau}_o$ and $\bar{\tau}_c$ can be recognized as the rate constants for the transitions between the channel open and closed states. The rate constants for the transitions between the stable states of a two-dimensional free energy surface like the one described here can be predicted by a recent theory of Berezhkovskii et al.⁴⁶ Either rate constant, e.g., $k_{o \rightarrow c}$ for the channel open-to-closed transition, can be written in the form

$$k_{o \rightarrow c} = \frac{k_L k_o}{k_L + k_o} \quad (15)$$

where k_L is the rate constant obtained by Langer⁴⁷ by assuming that the interwell transition is rate-limited by passage through the saddle point region and k_0 is the rate constant for the transition on the potential of mean force, $U_0(y)$, in y . The latter is defined via

$$e^{-U_0(y)} = C \int dx e^{-W(x,y)} \quad (16)$$

where C , like in eq 5, denotes an arbitrary constant. The Langer result is given by

$$k_L = \frac{\lambda}{2\pi} \left(\frac{\det \mathbf{K}_o}{|\det \mathbf{K}_{sp}|} \right)^{1/2} e^{-\Delta W_{o \rightarrow sp}} \quad (17)$$

where \mathbf{K} is the matrix of second derivatives of $W(x, y)$

$$\mathbf{K} = \begin{bmatrix} k_1 + \varepsilon(12x^2 - 2x - 4) & -k_1 \\ -k_1 & k_1 + k_b \end{bmatrix} \quad (18)$$

which is to be evaluated either at the channel open minimum (where $x = 1$) or at the saddle point (where $x = 0.076$). The remaining parameter λ in eq 17 is the absolute value of the only negative eigenvalue of the matrix $\mathbf{K}_{sp} \cdot \mathbf{D}$, where \mathbf{D} is the diffusion matrix, assumed here to be diagonal (with diagonal elements D_x and D_y).

As noted by Berezhkovskii et al.,⁴⁶ when $D_y \rightarrow 0$, motion along y , i.e., on the potential of mean force $U_0(y)$, becomes rate-limiting. This potential has a double-well shape, with one minimum at $y = 0$ corresponding to the channel open state and one minimum at $y = -0.91$ corresponding to the channel closed state, separated by a barrier at $y = -0.48$, to be denoted as y^\ddagger . The rate constant for the transition on $U_0(y)$ is given by

$$k_0 = \frac{D_y \int_{y < y^\ddagger} dy e^{-U_0(y)}}{2 \int_{y < y^\ddagger} dy e^{U_0(y)} \left[\int_{z < y} dz e^{-U_0(z)} \right]^2} \quad (19)$$

At $D_x = D_y = 2 \times 10^4$, $k_{o \rightarrow c}$ is rate-limited by k_L and the predicted value for its inverse is 6.4, which is close to the value of $\bar{\tau}_o$ obtained in the Brownian dynamics simulation. Similarly, the predicted value of 2.6 for the inverse of $k_{c \rightarrow o}$ is close to the simulation value of $\bar{\tau}_c$. Partial agonists will change both $k_{o \rightarrow c}$ and $k_{c \rightarrow o}$. For the blue free energy surface in Figure 2B modeling an NMDAR-type partial agonist, $\Delta W_{o \rightarrow sp}$ decreases while $\Delta W_{c \rightarrow sp}$ increases. Therefore, one should expect an increase in $k_{o \rightarrow c}$ and a decrease in $k_{c \rightarrow o}$.

DISCUSSION

We have presented a mechanism-based mathematical model that yields a number of thermodynamic and kinetic properties of iGluR gating. The model demonstrates that, by reducing either the degree of LBD closure (as in AMPA receptors) or the curvature of the LBD free energy basin (as in NMDA receptors), partial agonists can decrease the stabilization of the channel open state provided by agonist-induced LBD closure, thereby decreasing the channel open probability and thus agonist efficacy. With the model, we also derive a rigorous relation between the channel closed-to-open free energy difference and the tension within the LBD–TMC linker. Finally, by treating LBD closure and TMC opening as diffusive motions, we obtain gating trajectories that resemble single-channel recordings and calculate the rate constants for the transitions between the channel open and closed states.

In its present form, our model provides a conceptual framework for predicting functional observables from the energetics and dynamics of intra- and interdomain motions. The results presented are illustrative only, though the orders of magnitude for the channel open probability (~ 0.7), the energy barrier for channel opening or closing (~ 8 kcal/mol), and the mean residence time in the channel open or closed state (~ 5 ms) are in line with observed iGluR single-channel activity under certain conditions.^{13,16,48,49} The diffusion constants assumed here ($\sim 2 \times 10^4$ Å²/ms) for intradomain motions are approximately 500-fold smaller than the translational diffusion constant of a single-domain protein.⁵⁰ Kinetic studies on residue–residue contact formation in peptides have found slower intrachain diffusion relative to translational diffusion of free amino acids.⁵¹

It is worth noting that the free energy functions and the diffusion constants in the model can be obtained from molecular dynamics simulations. In fact, the free energy function for LBD closure has already been computed in several studies.^{28–30} Similar approaches can be used to obtain the free energy functions for TMC opening^{52–54} and for the linker extension. A number of important details will have to be accounted for. For example, the receptor contains four subunits. Here we treated the tetrameric TMC as a single unit but included only a single LBD monomer and the associated LBD–TMC linker. All four LBD monomers (perhaps with intersubunit coupling) and the associated linkers will have to be included. While we used a single coordinate here to represent the conformational freedom of the LBD or TMC, a more realistic representation may require more than one coordinate. Indeed, two coordinates were used for LBD closure in the recent free energy calculations.^{28–30} The TMC will likewise require at least two coordinates, e.g., lateral displacements of the A/C and B/D M3 helix C-termini. On the other hand, each LBD–TMC linker may still be modeled well by a single coordinate, i.e., the end-to-end extension, though the relation between this quantity and the LBD and TMC coordinates will not be as simple as the one presented here. In the end, one will be able to construct a high-dimensional free energy surface for the full receptor, from which thermodynamic properties like channel open probability and linker tension can be predicted. With diffusion constants of conformational coordinates calculated from additional simulations, prediction of kinetic properties of channel gating will also be possible.

Another direction for future development is to treat additional functional properties. Histograms of residence times from single-channel recordings on iGluR's at saturating agonist concentrations deviate from single exponentials, indicating multiple open and closed substates.^{11–16} The molecular basis for these multiple substates remains unclear. One possibility worth pursuing is that the channel-closed (or open) free energy basin encompasses multiple minima. In addition to the open and closed states, the receptor can enter a desensitized state in the continual presence of agonists. Channel desensitization can be accounted for by introducing a new free energy minimum for the LBD dimer^{17,19,27,55,56} or the TMC (LPW, unpublished data). It is also of both experimental and physiological interest to study channel gating evoked by a brief application of agonists, replicating what occurs at synapses. Treating this condition will require the consideration of agonist association and dissociation kinetics. Our modeling approach will facilitate mechanistic interpretation of functional data and guide the design of functional

experiments, on iGluR's as well as on other families of ligand-gated ion channels⁵⁷ and channel proteins in general.

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Notes

The authors declare no competing financial interest.

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ABBREVIATIONS

iGluR, ionotropic glutamate receptor; LBD, ligand-binding domain; TMC, transmembrane channel

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